

Second Fundamental Theorem Of Calculus

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Questions in past papers often come up combined with other topics.

Topic tags have been given for each question to enable you to know if you can do the question or whether you need to wait to cover the additional topic(s).

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Qualification: AP Calculus AB

Areas: Integration, Applications of Differentiation, Differential Equations

Subtopics: Global or Absolute Minima and Maxima, Modelling Situations, Integration Technique - Harder Powers, Accumulation of Change, Total Amount, Fundamental Theorem of Calculus (Second)

Paper: Part B-Non-Calc / Series: 2000 / Difficulty: Medium / Question Number: 4

- 4. Water is pumped into an underground tank at a constant rate of 8 gallons per minute. Water leaks out of the tank at the rate of $\sqrt{t+1}$ gallons per minute, for $0 \le t \le 120$ minutes. At time t=0, the tank contains 30 gallons of
 - (a) How many gallons of water leak out of the tank from time t = 0 to t = 3 minutes?
 - (b) How many gallons of water are in the tank at time t = 3 minutes?
 - (c) Write an expression for A(t), the total number of gallons of water in the tank at time t.
 - (d) At what time t, for $0 \le t \le 120$, is the amount of water in the tank a maximum? Justify your answer.



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Qualification: AP Calculus AB

Areas: Applications of Integration, Applications of Differentiation, Integration

Subtopics: Interpreting Meaning in Applied Contexts, Total Amount, Increasing/Decreasing, Fundamental Theorem of Calculus (Second), Global or Absolute Minima and Maxima,

Accumulation of Change

Paper: Part A-Calc / Series: 2002 / Difficulty: Hard / Question Number: 2

2. The rate at which people enter an amusement park on a given day is modeled by the function E defined by

$$E(t) = \frac{15600}{\left(t^2 - 24t + 160\right)}.$$

The rate at which people leave the same amusement park on the same day is modeled by the function Ldefined by

$$L(t) = \frac{9890}{\left(t^2 - 38t + 370\right)}.$$

Both E(t) and L(t) are measured in people per hour and time t is measured in hours after midnight. These functions are valid for $9 \le t \le 23$, the hours during which the park is open. At time t = 9, there are no people in the park.

- (a) How many people have entered the park by 5:00 P.M. (t = 17)? Round your answer to the nearest whole number.
- (b) The price of admission to the park is \$15 until 5:00 P.M. (t = 17). After 5:00 P.M., the price of admission to the park is \$11. How many dollars are collected from admissions to the park on the given day? Round your answer to the nearest whole number.
- (c) Let $H(t) = \int_0^t (E(x) L(x)) dx$ for $9 \le t \le 23$. The value of H(17) to the nearest whole number is 3725. Find the value of H'(17), and explain the meaning of H(17) and H'(17) in the context of the amusement
- (d) At what time t, for $9 \le t \le 23$, does the model predict that the number of people in the park is a maximum?



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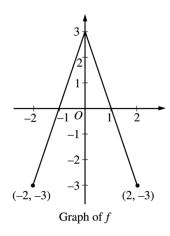
Qualification: AP Calculus AB

Areas: Differentiation, Integration, Applications of Differentiation

Subtopics: Fundamental Theorem of Calculus (Second), Integration Technique – Geometric Areas, Derivative Graphs, Integration - Area Under A Curve, Increasing/Decreasing

Concavity, Integration Graphs

Paper: Part B-Non-Calc / Series: 2002 / Difficulty: Hard / Question Number: 4



- 4. The graph of the function f shown above consists of two line segments. Let g be the function given by $g(x) = \int_0^x f(t) dt$.
 - (a) Find g(-1), g'(-1), and g''(-1).
 - (b) For what values of x in the open interval (-2, 2) is g increasing? Explain your reasoning.
 - (c) For what values of x in the open interval (-2, 2) is the graph of g concave down? Explain your reasoning.
 - (d) On the axes provided, sketch the graph of g on the closed interval [-2, 2]. (Note: The axes are provided in the pink test booklet only.)

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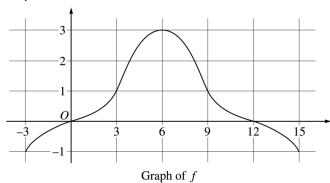


Qualification: AP Calculus AB

Areas: Integration, Applications of Integration, Applications of Differentiation, Differentiation

Subtopics: Fundamental Theorem of Calculus (Second), Derivative Graphs, Concavity, Increasing/Decreasing, Riemann Sums - Trapezoidal Rule

Paper: Part B-Non-Calc / Series: 2002-Form-B / Difficulty: Medium / Question Number: 4



- 4. The graph of a differentiable function f on the closed interval [-3, 15] is shown in the figure above. The graph of f has a horizontal tangent line at x = 6. Let $g(x) = 5 + \int_6^x f(t)dt$ for $-3 \le x \le 15$.
 - (a) Find g(6), g'(6), and g''(6).
 - (b) On what intervals is g decreasing? Justify your answer.
 - (c) On what intervals is the graph of g concave down? Justify your answer.
 - (d) Find a trapezoidal approximation of $\int_{-3}^{15} f(t) dt$ using six subintervals of length $\Delta t = 3$.

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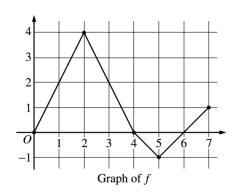
Qualification: AP Calculus AB

Areas: Integration, Differentiation, Applications of Differentiation

Subtopics: Derivative Graphs, Rates of Change (Average), Mean Value Theorem, Points Of Inflection, Integration Technique - Geometric Areas, Fundamental Theorem of Calculus

(Second), Integration Graphs

Paper: Part B-Non-Calc / Series: 2003-Form-B / Difficulty: Medium / Question Number: 5



- 5. Let f be a function defined on the closed interval [0, 7]. The graph of f, consisting of four line segments, is shown above. Let g be the function given by $g(x) = \int_2^x f(t) dt$.
 - (a) Find g(3), g'(3), and g''(3).
 - (b) Find the average rate of change of g on the interval $0 \le x \le 3$.
 - (c) For how many values c, where 0 < c < 3, is g'(c) equal to the average rate found in part (b)? Explain your reasoning.
 - (d) Find the x-coordinate of each point of inflection of the graph of g on the interval 0 < x < 7. Justify your



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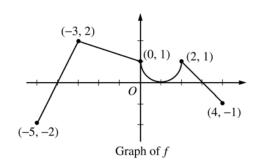


Qualification: AP Calculus AB

Areas: Applications of Differentiation, Integration

Subtopics: Derivative Graphs, Fundamental Theorem of Calculus (Second), Integration Technique – Geometric Areas, Local or Relative Minima and Maxima, Global or Absolute Minima and Maxima, Points Of Inflection, Integration Graphs

Paper: Part B-Non-Calc / Series: 2004 / Difficulty: Somewhat Challenging / Question Number: 5



- 5. The graph of the function f shown above consists of a semicircle and three line segments. Let g be the function given by $g(x) = \int_{-3}^{x} f(t) dt$.
 - (a) Find g(0) and g'(0).
 - (b) Find all values of x in the open interval (-5, 4) at which g attains a relative maximum. Justify your answer.
 - (c) Find the absolute minimum value of g on the closed interval [-5, 4]. Justify your answer.
 - (d) Find all values of x in the open interval (-5, 4) at which the graph of g has a point of inflection.

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Qualification: AP Calculus AB

Areas: Applications of Differentiation, Differentiation, Integration

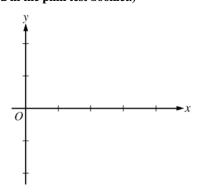
Subtopics: Local or Relative Minima and Maxima, Derivative Tables, Derivative Graphs, Fundamental Theorem of Calculus (Second), Points Of Inflection, Increasing/Decreasing

Paper: Part B-Non-Calc / Series: 2005 / Difficulty: Somewhat Challenging / Question Number: 4

x	0	0 < x < 1	1	1 < <i>x</i> < 2	2	2 < x < 3	3	3 < x < 4
f(x)	-1	Negative	0	Positive	2	Positive	0	Negative
f'(x)	4	Positive	0	Positive	DNE	Negative	-3	Negative
f''(x)	-2	Negative	0	Positive	DNE	Negative	0	Positive

- 4. Let f be a function that is continuous on the interval [0, 4). The function f is twice differentiable except at x = 2. The function f and its derivatives have the properties indicated in the table above, where DNE indicates that the derivatives of f do not exist at x = 2.
 - (a) For 0 < x < 4, find all values of x at which f has a relative extremum. Determine whether f has a relative maximum or a relative minimum at each of these values. Justify your answer.
 - (b) On the axes provided, sketch the graph of a function that has all the characteristics of f.

(Note: Use the axes provided in the pink test booklet.)



- (c) Let g be the function defined by $g(x) = \int_1^x f(t) dt$ on the open interval (0, 4). For 0 < x < 4, find all values of x at which g has a relative extremum. Determine whether g has a relative maximum or a relative minimum at each of these values. Justify your answer.
- (d) For the function g defined in part (c), find all values of x, for 0 < x < 4, at which the graph of g has a point of inflection. Justify your answer.

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Question 8

Qualification: AP Calculus AB

Areas: Applications of Differentiation, Integration

Subtopics: Fundamental Theorem of Calculus (Second), Points Of Inflection, Increasing/Decreasing, Integration Technique – Geometric Areas, Derivative Graphs, Integration Graphs

Company of Calculus (Second), Points Of Inflection, Increasing/Decreasing, Integration Technique – Geometric Areas, Derivative Graphs, Integration Graphs

Company of Calculus (Second), Points Of Inflection, Increasing/Decreasing, Integration Technique – Geometric Areas, Derivative Graphs, Integration Graphs

Company of Calculus (Second), Points Of Inflection, Increasing/Decreasing, Integration Technique – Geometric Areas, Derivative Graphs, Integration Graphs

Company of Calculus (Second), Points Of Inflection, Increasing/Decreasing, Integration Technique – Geometric Areas, Derivative Graphs, Integration Graphs

Company of Calculus (Second), Points Of Inflection, Increasing/Decreasing, Integration Technique – Geometric Areas, Derivative Graphs, Integration Graphs

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Company of Calculus (Second), Points Of Inflection, Increasing/Decreasing, Integration Technique – Geometric Areas, Derivative Graphs, Integration Graphs

Company of Calculus (Second), Points Of Inflection, Increasing/Decreasing, Integration Graphs

Company of Calculus (Second), Points Of Inflection, Increasing/Decreasing, Integration Graphs

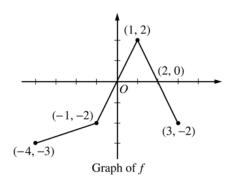
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Company of Calculus (Second), Points Of Inflection, Increasing, Integration Graphs

Company of Calculus (Second), Points Of Inflection, Increasing, Integration Graphs

Company of Calculus (Second), Points Of Inflection, Increasing, Integration Gra

Paper: Part B-Non-Calc / Series: 2005-Form-B / Difficulty: Somewhat Challenging / Question Number: 4



- 4. The graph of the function f above consists of three line segments.
 - (a) Let g be the function given by $g(x) = \int_{-4}^{x} f(t) dt$. For each of g(-1), g'(-1), and g''(-1), find the value or state that it does not exist.
 - (b) For the function g defined in part (a), find the x-coordinate of each point of inflection of the graph of g on the open interval -4 < x < 3. Explain your reasoning.
 - (c) Let h be the function given by $h(x) = \int_{x}^{3} f(t) dt$. Find all values of x in the closed interval $-4 \le x \le 3$ for which h(x) = 0.
 - (d) For the function h defined in part (c), find all intervals on which h is decreasing. Explain your reasoning.

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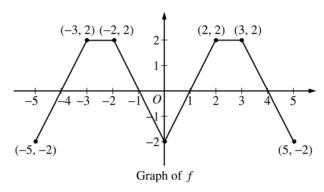


Qualification: AP Calculus AB

Areas: Applications of Integration, Applications of Differentiation

Subtopics: Derivative Graphs, Fundamental Theorem of Calculus (Second), Local or Relative Minima and Maxima, Tangents To Curves

Paper: Part A-Calc / Series: 2006 / Difficulty: Hard / Question Number: 3



- 3. The graph of the function f shown above consists of six line segments. Let g be the function given by $g(x) = \int_0^x f(t) dt$.
 - (a) Find g(4), g'(4), and g''(4).
 - (b) Does g have a relative minimum, a relative maximum, or neither at x = 1? Justify your answer.
 - (c) Suppose that f is defined for all real numbers x and is periodic with a period of length 5. The graph above shows two periods of f. Given that g(5) = 2, find g(10) and write an equation for the line tangent to the graph of g at x = 108.

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Qualification: AP Calculus AB

Areas: Limits and Continuity, Applications of Differentiation, Integration

Subtopics: Intermediate Value Theorem, Mean Value Theorem, Fundamental Theorem of Calculus (Second), Tangents To Curves, Derivative Tables

Paper: Part A-Calc / Series: 2007 / Difficulty: Very Hard / Question Number: 3

x	f(x)	f'(x)	g(x)	g'(x)
1	6	4	2	5
2	9	2	3	1
3	10	-4	4	2
4	-1	3	6	7

- 3. The functions f and g are differentiable for all real numbers, and g is strictly increasing. The table above gives values of the functions and their first derivatives at selected values of x. The function h is given by h(x) = f(g(x)) 6.
 - (a) Explain why there must be a value r for 1 < r < 3 such that h(r) = -5.
 - (b) Explain why there must be a value c for 1 < c < 3 such that h'(c) = -5.
 - (c) Let w be the function given by $w(x) = \int_1^{g(x)} f(t) dt$. Find the value of w'(3).
 - (d) If g^{-1} is the inverse function of g, write an equation for the line tangent to the graph of $y = g^{-1}(x)$ at x = 2.

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Qualification: AP Calculus AB

Areas: Applications of Differentiation, Differentiation

Subtopics: Fundamental Theorem of Calculus (Second), Differentiation Technique - Chain Rule, Differentiation Technique - Trigonometry, Tangents To Curves, Global or Absolute

Minima and Maxima

Paper: Part B-Non-Calc / Series: 2008-Form-B / Difficulty: Easy / Question Number: 4

- 4. The functions f and g are given by $f(x) = \int_0^{3x} \sqrt{4 + t^2} \ dt$ and $g(x) = f(\sin x)$.
 - (a) Find f'(x) and g'(x).
 - (b) Write an equation for the line tangent to the graph of y = g(x) at $x = \pi$.
 - (c) Write, but do not evaluate, an integral expression that represents the maximum value of g on the interval $0 \le x \le \pi$. Justify your answer.

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Qualification: AP Calculus AB

Areas: Applications of Differentiation

Subtopics: Modelling Situations, Interpreting Meaning in Applied Contexts, Fundamental Theorem of Calculus (Second), Global or Absolute Minima and Maxima, Local or Relative

Minima and Maxima

Paper: Part A-Calc / Series: 2009 / Difficulty: Somewhat Challenging / Question Number: 3

- 3. Mighty Cable Company manufactures cable that sells for \$120 per meter. For a cable of fixed length, the cost of producing a portion of the cable varies with its distance from the beginning of the cable. Mighty reports that the cost to produce a portion of a cable that is x meters from the beginning of the cable is 6√x dollars per meter. (Note: Profit is defined to be the difference between the amount of money received by the company for selling the cable and the company's cost of producing the cable.)
 - (a) Find Mighty's profit on the sale of a 25-meter cable.
 - (b) Using correct units, explain the meaning of $\int_{25}^{30} 6\sqrt{x} \ dx$ in the context of this problem.
 - (c) Write an expression, involving an integral, that represents Mighty's profit on the sale of a cable that is k meters long.
 - (d) Find the maximum profit that Mighty could earn on the sale of one cable. Justify your answer.



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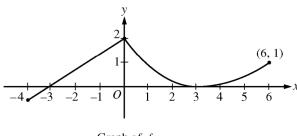
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Qualification: AP Calculus AB

Areas: Limits and Continuity, Applications of Differentiation

Subtopics: Differentiability, Rates of Change (Average), Mean Value Theorem, Concavity, Fundamental Theorem of Calculus (Second)

Paper: Part A-Calc / Series: 2009-Form-B / Difficulty: Somewhat Challenging / Question Number: 3



Graph of f

- 3. A continuous function f is defined on the closed interval $-4 \le x \le 6$. The graph of f consists of a line segment and a curve that is tangent to the x-axis at x = 3, as shown in the figure above. On the interval 0 < x < 6, the function f is twice differentiable, with f''(x) > 0.
 - (a) Is f differentiable at x = 0? Use the definition of the derivative with one-sided limits to justify your answer.
 - (b) For how many values of $a, -4 \le a < 6$, is the average rate of change of f on the interval [a, 6] equal to 0? Give a reason for your answer.
 - (c) Is there a value of $a, -4 \le a < 6$, for which the Mean Value Theorem, applied to the interval [a, 6], guarantees a value c, a < c < 6, at which $f'(c) = \frac{1}{3}$? Justify your answer.
 - (d) The function g is defined by $g(x) = \int_0^x f(t) dt$ for $-4 \le x \le 6$. On what intervals contained in [-4, 6]is the graph of g concave up? Explain your reasoning.



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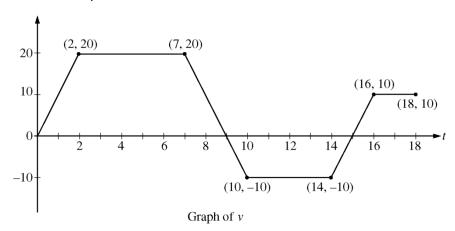


Qualification: AP Calculus AB

Areas: Applications of Integration, Applications of Differentiation, Integration

Subtopics: Kinematics (Displacement, Velocity, and Acceleration), Global or Absolute Minima and Maxima, Derivative Graphs, Integration Technique – Geometric Areas, Fundamental Theorem of Calculus (Second)

Paper: Part B-Non-Calc / Series: 2010-Form-B / Difficulty: Medium / Question Number: 4



- 4. A squirrel starts at building A at time t = 0 and travels along a straight, horizontal wire connected to building B. For $0 \le t \le 18$, the squirrel's velocity is modeled by the piecewise-linear function defined by the graph above.
 - (a) At what times in the interval 0 < t < 18, if any, does the squirrel change direction? Give a reason for your answer.
 - (b) At what time in the interval $0 \le t \le 18$ is the squirrel farthest from building A? How far from building A is the squirrel at that time?
 - (c) Find the total distance the squirrel travels during the time interval $0 \le t \le 18$.
 - (d) Write expressions for the squirrel's acceleration a(t), velocity v(t), and distance x(t) from building A that are valid for the time interval 7 < t < 10.

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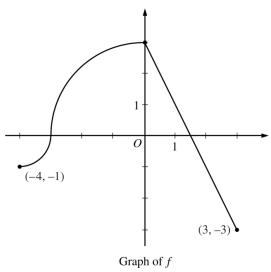


Qualification: AP Calculus AB

Areas: Applications of Differentiation

Subtopics: Fundamental Theorem of Calculus (Second), Global or Absolute Minima and Maxima, Points Of Inflection, Rates of Change (Average), Mean Value Theorem

Paper: Part B-Non-Calc / Series: 2011 / Difficulty: Easy / Question Number: 4



- 4. The continuous function f is defined on the interval $-4 \le x \le 3$. The graph of f consists of two quarter circles and one line segment, as shown in the figure above. Let $g(x) = 2x + \int_0^x f(t) dt$.
 - (a) Find g(-3). Find g'(x) and evaluate g'(-3).
 - (b) Determine the x-coordinate of the point at which g has an absolute maximum on the interval $-4 \le x \le 3$. Justify your answer.
 - (c) Find all values of x on the interval -4 < x < 3 for which the graph of g has a point of inflection. Give a reason for your answer.
 - (d) Find the average rate of change of f on the interval $-4 \le x \le 3$. There is no point c, -4 < c < 3, for which f'(c) is equal to that average rate of change. Explain why this statement does not contradict the Mean Value Theorem.

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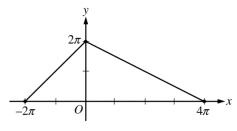


Qualification: AP Calculus AB

Areas: Applications of Differentiation, Integration

Subtopics: Integration Technique – Geometric Areas, Local or Relative Minima and Maxima, Differentiation Technique – Trigonometry, Fundamental Theorem of Calculus (Second)

Paper: Part B-Non-Calc / Series: 2011-Form-B / Difficulty: Somewhat Challenging / Question Number: 6



Graph of g

- 6. Let g be the piecewise-linear function defined on $[-2\pi, 4\pi]$ whose graph is given above, and let $f(x) = g(x) - \cos\left(\frac{x}{2}\right)$.
 - (a) Find $\int_{-2\pi}^{4\pi} f(x) dx$. Show the computations that lead to your answer.
 - (b) Find all x-values in the open interval $(-2\pi, 4\pi)$ for which f has a critical point.
 - (c) Let $h(x) = \int_0^{3x} g(t) dt$. Find $h'\left(-\frac{\pi}{3}\right)$.



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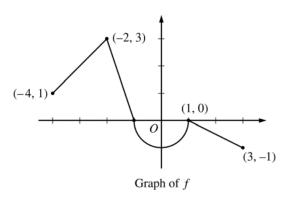
Qualification: AP Calculus AB

Areas: Applications of Differentiation

Subtopics: Integration Technique – Geometric Areas, Fundamental Theorem of Calculus (Second), Local or Relative Minima and Maxima, Points Of Inflection, Derivative Graphs,

Integration Graphs

Paper: Part B-Non-Calc / Series: 2012 / Difficulty: Medium / Question Number: 3



- 3. Let f be the continuous function defined on [-4, 3] whose graph, consisting of three line segments and a semicircle centered at the origin, is given above. Let g be the function given by $g(x) = \int_1^x f(t) dt$.
 - (a) Find the values of g(2) and g(-2).
 - (b) For each of g'(-3) and g''(-3), find the value or state that it does not exist.
 - (c) Find the x-coordinate of each point at which the graph of g has a horizontal tangent line. For each of these points, determine whether g has a relative minimum, relative maximum, or neither a minimum nor a maximum at the point. Justify your answers.
 - (d) For -4 < x < 3, find all values of x for which the graph of g has a point of inflection. Explain your reasoning.

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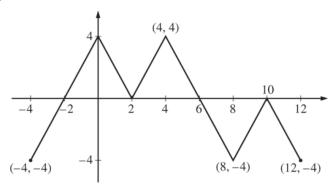
Qualification: AP Calculus AB

Areas: Applications of Differentiation

Subtopics: Local or Relative Minima and Maxima, Fundamental Theorem of Calculus (Second), Points Of Inflection, Global or Absolute Minima and Maxima, Derivative Graphs,

Integration Graphs

Paper: Part B-Non-Calc / Series: 2016 / Difficulty: Medium / Question Number: 3



Graph of f

- 3. The figure above shows the graph of the piecewise-linear function f. For $-4 \le x \le 12$, the function g is defined by $g(x) = \int_2^x f(t) dt$.
 - (a) Does g have a relative minimum, a relative maximum, or neither at x = 10? Justify your answer.
 - (b) Does the graph of g have a point of inflection at x = 4? Justify your answer.
 - (c) Find the absolute minimum value and the absolute maximum value of g on the interval $-4 \le x \le 12$. Justify your answers.
 - (d) For $-4 \le x \le 12$, find all intervals for which $g(x) \le 0$.

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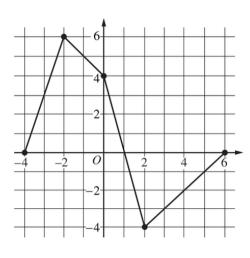


Qualification: AP Calculus AB

Areas: Applications of Differentiation, Integration

Subtopics: Concavity, Fundamental Theorem of Calculus (Second), Differentiation Technique – Product Rule, L'Hôpital's Rule, Mean Value Theorem, Rates of Change (Average), Integration Technique – Geometric Areas, Integration Graphs

Paper: Part B-Non-Calc / Series: 2021 / Difficulty: Somewhat Challenging / Question Number: 4



Graph of f

- 4. Let f be a continuous function defined on the closed interval $-4 \le x \le 6$. The graph of f, consisting of four line segments, is shown above. Let G be the function defined by $G(x) = \int_0^x f(t) dt$.
 - (a) On what open intervals is the graph of G concave up? Give a reason for your answer.
 - (b) Let P be the function defined by $P(x) = G(x) \cdot f(x)$. Find P'(3).
 - (c) Find $\lim_{x\to 2} \frac{G(x)}{x^2 2x}$.
 - (d) Find the average rate of change of G on the interval [-4, 2]. Does the Mean Value Theorem guarantee a value c, -4 < c < 2, for which G'(c) is equal to this average rate of change? Justify your answer.

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Qualification: AP Calculus AB

Areas: Applications of Differentiation, Applications of Integration

Subtopics: Total Amount, Average Value of a Function, Increasing/Decreasing, Global or Absolute Minima and Maxima, Fundamental Theorem of Calculus (Second), Accumulation

of Change

Paper: Part A-Calc / Series: 2022 / Difficulty: Easy / Question Number: 1

- 1. From 5 A.M. to 10 A.M., the rate at which vehicles arrive at a certain toll plaza is given by $A(t) = 450\sqrt{\sin(0.62t)}$, where t is the number of hours after 5 A.M. and A(t) is measured in vehicles per hour. Traffic is flowing smoothly at 5 A.M. with no vehicles waiting in line.
 - (a) Write, but do not evaluate, an integral expression that gives the total number of vehicles that arrive at the toll plaza from 6 A.M. (t = 1) to 10 A.M. (t = 5).
 - (b) Find the average value of the rate, in vehicles per hour, at which vehicles arrive at the toll plaza from 6 A.M. (t = 1) to 10 A.M. (t = 5).
 - (c) Is the rate at which vehicles arrive at the toll plaza at 6 A.M. (t = 1) increasing or decreasing? Give a reason for your answer.
 - (d) A line forms whenever $A(t) \ge 400$. The number of vehicles in line at time t, for $a \le t \le 4$, is given by $N(t) = \int_a^t (A(x) 400) \ dx$, where a is the time when a line first begins to form. To the nearest whole number, find the greatest number of vehicles in line at the toll plaza in the time interval $a \le t \le 4$. Justify your answer.

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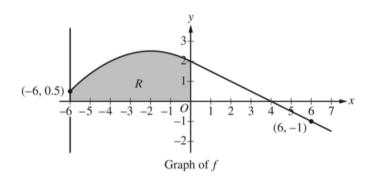
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Qualification: AP Calculus AB

Areas: Applications of Differentiation, Differentiation

Subtopics: Integration Technique - Geometric Areas, Local or Relative Minima and Maxima, Fundamental Theorem of Calculus (Second), Derivative Graphs, Integration Graphs

Paper: Part B-Non-Calc / Series: 2024 / Difficulty: Medium / Question Number: 4



- 4. The graph of the differentiable function f, shown for $-6 \le x \le 7$, has a horizontal tangent at x = -2 and is linear for $0 \le x \le 7$. Let R be the region in the second quadrant bounded by the graph of f, the vertical line x = -6, and the x- and y-axes. Region R has area 12.
 - (a) The function g is defined by $g(x) = \int_0^x f(t) dt$. Find the values of g(-6), g(4), and g(6).
 - (b) For the function g defined in part (a), find all values of x in the interval $0 \le x \le 6$ at which the graph of g has a critical point. Give a reason for your answer.
 - (c) The function h is defined by $h(x) = \int_{-6}^{x} f'(t) dt$. Find the values of h(6), h'(6), and h''(6). Show the work that leads to your answers.

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